Imperative programming with Python
January 2012 project: Class #3

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Functions: DIY

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```
def is_even(n):
    if n % 2 == 0:
        return True
    else:
        return False
```

- The argument passed to `is_even(n)` will be assigned to `n`.

- The `return` keyword sets the return value and exits the function immediately. It can also be used without a value (just `return`).

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        return False
```

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- The `return` keyword sets the return value and exits the function immediately. It can also be used without a value (just `return`).

- *Good practice tip*: reduce the number of return points. If possible, have only one.

```
def is_even(n):
    return (n % 2 == 0)
```

Functions: local variables

- Variables inside function definitions have a *local* scope.

```
def average(n, m):
    thesum = float(n + m)
    return thesum/2
```

- You can only use the function as a *black box*

```
>>> print average(3,4)
3.5
>>> print thesum
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
NameError: name 'thesum' is not defined
```

- Design tip: thinking of functions as black boxes performing a certain action is the way to go.

Functions: execution and the call stack

▶
```
def cat_twice_and_print(part1, part2):
    cat = part1 + part2
    print_twice(cat)

def print_twice(msg):
    print msg
    print msg

line1 = 'welcome␣'
line2 = 'to␣the␣jungle'
cat_twice_and_print(line1, line2)
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def cat_twice_and_print (part1 , part2):
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Output:

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welcome to the jungle
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Functions: recursion

- Functions can call *themselves* in their definition.

```python
# calculates n * m (in a complicated way)
def multiply(n, m):
    if n == 0:
        return 0
    else:
        return m + multiply(n - 1, m)
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> $ret \mapsto 7 + \ldots$

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multiply
n ↦ 2, m ↦ 7
ret ↦ 7 + . . .

multiply
n ↦ 1, m ↦ 7
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multiply
$n \mapsto 2$, $m \mapsto 7$
ret $\mapsto 7 + \ldots$

multiply
$n \mapsto 1$, $m \mapsto 7$
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multiply
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ret $\mapsto 0$

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$ret \mapsto 7 + 0 = 7$

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  multiply
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Functions: recursion

- It is crucial that the arguments of a recursive call are in some sense 'smaller' than the arguments of the function call itself.
- What happens if we write multiply as follows

```python
def multiply(n, m):
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Functions: recursion

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- What happens if we write `multiply` as follows

```python
def multiply(n, m):
    if n == 0:
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```

```
>>> multiply(2, 7)
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
  File "<stdin>", line 5, in multiply
  File "<stdin>", line 5, in multiply
...
  File "<stdin>", line 5, in multiply
RuntimeError: maximum recursion depth exceeded
```

- Stack overflow!

Functions: recursion

- You can also have many recursive calls

```
def fib(n):
    if n == 0:
        return n
    else:
        return fib(n - 1) + fib(n - 2)
```

- Is it well defined?

Functions: recursion

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    if n == 0:
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def fib(n):
    if n == 0 or n == 1:
        return n
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def fib(n):
    if n == 0 or n == 1:
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```

- Is it well defined? Yes.

Functions: recursion

- The argument itself *can* increase. . .

```
def reverse_string(s):
    return reverse_from_n(s, 0)

def reverse_from_n(s, i):
    if i == len(s):
        return ''
    else:
        return reverse_from_n(s, i+1) + s[i]
```

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```
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    if i == len(s):
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```

- But if you look closer `len(s) - i` is strictly decreasing.

Functions: recursion

- Is the following function well defined (for $n > 0$)?

```python
def collatz(n):
    if n == 1:
        return 0
    elif n % 2 == 0:
        return 1 + collatz(n/2)
    else:
        return 1 + collatz(3*n+1)
```

Functions: recursion
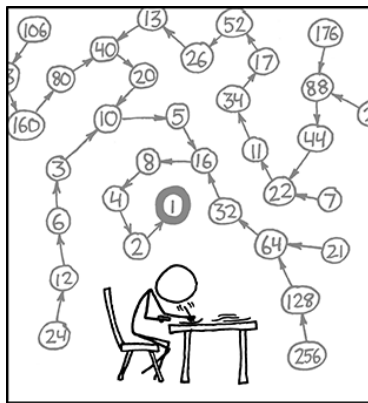
- Is the folowing function well defined (for $n > 0$)?

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    if n == 1:
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```

- Who knows! It has been an open problem for years.

The collatz conjecture

Repetition

- Suppose we want to make a function that given *n* calculates $\sum_{i=1}^{n} i$.

```
def sum_up_to(n):
    res = 1 + 2 + ... + n
    return res
```

This is not a valid program, for many reasons.

Repetition

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def sum_up_to(n):
    res = 1 + 2 + ... + n
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This is not a valid program, for many reasons.

- Luckily, computers are very good at doing repetitive things. We have the while statement to aid us.

```
def sum_up_to(n):
    i = 1
    v = 0
    while i <= n:
        v = v + i
        i = i + 1
    return v
```

The body gets repeated while the condition evaluates to *true*.

Repetition

- Another handy construction is the `for` statement
- It goes through so called 'iterable' objects, e.g. strings

```
>>> for letter in 'hello':
...     print 'Give me an "' + letter + '"!'
...
Give me an "h"!
Give me an "e"!
Give me an "l"!
Give me an "l"!
Give me an "o"!
```

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- 'Lists' are also iterable (we will see them later)

```
>>> range(3)
[0, 1, 2]
>>> for i in range(3):
...     print i**2
...
0
1
4
```

Repetition: while loops

- `while` loops are a powerful but tricky construction.

- They can run forever and make our program hang!

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while True:
    x = x + 1
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while True:
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ok, we would not write that, but what about...

```
x = int(raw_input())
sum = 0
while x != 100:
    sum = sum + x
    x = x + 2
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x = int ( raw_input ())
sum = 0
while x != 100:
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```

- If $x > 100$ or x is odd this loop never ends.

Repetition: loop invariants

- A *loop invariant* is an invariant used to prove properties of loops.
- For example, correctness and termination of loops.
- Connected to pre and post-conditions.

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E.g.: `count(c:String, sentence:String) → res:Int`

- pre: True
- post: $res = |[1 : i \in \{0, \ldots, |sentence| - 1\}, \texttt{sentence}_i = \texttt{c}]|$

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Suppose we have the following implementation

```
def count(c, sentence):
    i = 0; n = 0
    while i < len(sentence):
        if sentence[i] == c: n = n + 1
        i = i + 1
    return n
```

Repetition: loop invariants

post: $res = |[1 : i \in \{0, \ldots, |sentence| - 1\}, \mathrm{sentence}_i = \mathrm{c}]|$

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Let **C** be our loop condition and **I** be our loop invariant, a theorem says:

$$\frac{\{C \wedge I\} \; \text{body} \; \{I\}}{\{I\} \; \textbf{while} \; (C) \; \text{body} \; \{\neg C \wedge I\}}$$

- **C:**

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- **I:** $0 \leq i \leq |\mathtt{sentence}| \wedge n = |[1 : x \in \{0, \ldots, i-1\}, \mathtt{sentence}_x = \mathtt{c}]|$

If we chose correctly our invariant, with $\neg C \wedge I$ we should be able to prove the postcondition.

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Long answer:

- In old languages like BASIC and Pascal the `for` statement was meant to be used as `for i = A to B: body`. Modifications to `i` in the body would not change the iteration.
- In a `while` statement, the expression gets evaluated in every loop.

Repetition: where's the catch?

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Long answer:

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Some facts (check this out):

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- But, if you don't use `while` you can only write 'some' of them.
- In fact, you could write any program using just ONE `while`.

The estimation game

- Building software in the real world is a lot about planning.
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- Average pages of an ILLC MoL thesis $\rightarrow$ 77.

References

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